Progression in Fractions, Decimals, Percentages, Ratio & Proportion

Year Group	Knowledge and Skills	Vocabulary
-	Supporting Resource: Maths No Problem	
	Essential & most valuable knowledge for the next key stage is highlighted in yellow	
Nursery	N/A	
Reception	N/A	
Year 1	Fractions	half
	• To split an object (shape) into two equal parts; to identify shapes that have been split into two equal parts.	halve
	 To split an object (shape) into four equal parts; to identify shapes that have been split into four equal parts. 	quarter
	 To share and group objects into halves and quarters; to determine half of a number and a quarter of a number. 	same parts
		group
	<u>Y1 National Curriculum – End Point:</u>	Broad
	Pupils will be taught to:	
	 recognise, find and name a half as one of two equal parts of an object, shape or quantity 	
	- recognise, find and name a quarter as one of four equal parts of an object, shape or quantity	
Year 2	Fractions	All of the above, plus:
	 To make equal parts from a whole using simple and complex methods. 	
	 To show and recognise halves and quarters. 	part
	 To show and identify more than one quarter using materials and pictures. 	equal parts fraction
	 To show and identify thirds in shapes; to use the vocabulary 'numerator' and 'denominator' when referring to 	one whole
	fractions.	one half
	 To identify and name fractions by looking at the number of pieces and how many are shaded in. 	two halves
	 To recognise equivalent fractions in quarters, thirds and halves. 	one quarter
	 To compare and order similar fractions by looking at the size of the pieces shaded. 	two three four quarters
	 To compare and order fractions with different denominators. 	
	 To count the number of wholes and parts to form mixed numbers. 	
	 To count in halves and place halves onto a number line using pictures. 	
	 To count in quarters and place quarters onto a number line using pictures. 	
	 To count in thirds and place thirds onto a number line using pictures. 	
	 To find fractions (half) of whole numbers. 	
	• To find a fraction (third) of a whole number.	
	• To find a fraction (quarter) of a number.	

	 To find a fraction (half, third, quarter) of a quantity (length) 	
	Y2 National Curriculum – End Point:	
	Pupils will be taught to:	
	• recognise, find, name and write fractions $\frac{1}{3}$, $\frac{1}{4}$, $\frac{2}{4}$ and $\frac{3}{4}$ of a length, shape, set of	
	objects or quantity	
	• write simple fractions for example, $\frac{1}{2}$ of 6 = 3 and recognise the equivalence of $\frac{2}{4}$	
	and $\frac{1}{2}$.	
Year 3	Fractions	All of the above, plus:
	 To count in tenths; to recognise tenths and be able to determine how many tenths are shaded. 	
	 To make number pairs to create 1; to combine fractions to make 1. 	one third
	 To add fractions with the same denominator. 	two thirds
	• To consolidate adding fractions with the same name; to learn how fractions can add to 1.	three thirds
	 To subtract fractions with the same name. 	one tenth equivalent
	 To find equivalent fractions through paper folding and shading. 	number line
	 To find equivalent fractions using paper folding and shading. 	numerator
	• To find equivalent fractions; to place fractions on a number line.	denominator
	• To find fractions equivalent to 1/2; to use pictorial representations and multiplication to show equivalence.	
	• To find equivalent fractions using concrete objects and pictorial representations.	
	 To find equivalent fractions using pictorial representations and multiplication. 	
	 To find the simplest fraction using visualisation and concrete materials. 	
	 To find the simplest fraction using pictorial representations and division. 	
	• To find equivalent fractions using multiplication and division; to determine whether or not a fraction is equivalent.	
	 To compare the fractions 1/2 and 1/4 using pictorial representations and concrete materials 	
	 To compare fractions using pictorial representations; to understand the numerical nature of the numerator. 	
	 To compare fractions with different names (denominators) using pictorial representations and number lines. 	
	 To add fractions using pictorial representations; to simplify fractions after adding them. 	
	 To subtract fractions using pictorial representations; to simplify fractions after they have been subtracted. 	
	 To subtract fractions from a whole amount; to use pictorial representations of whole numbers to help subtract 	
	fractions.	
	 To determine a fraction of a whole number using pictorial representations. 	
	• To find a fraction of a whole number using pictorial representations, multiplication and concrete objects.	
	 To consolidate finding the fraction of a whole number. 	

	 To divide 1 between more than 1; to share 1 whole equally between more than 1. To share more than 1 using pictorial representations and division. To share more than 1; to recognise a whole and its parts using pictures and number lines. To show more than 1 whole after sharing a number of items equally; to use pictorial representations to share whole items equally. To apply bar modelling to represent fractions in word problems; to solve word problems using pictorial representations and abstract methods. To use bar models to solve word problems involving the fractions 1/ 2 and 1/ 	
	 Y3 National Curriculum – End Point: Pupils will be taught to: count up and down in tenths; recognise that tenths arise from dividing an object into 10 equal parts and in dividing one-digit numbers or quantities by 10 recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators recognise and use fractions as numbers: unit fractions and non-unit fractions with small denominators add and subtract fractions with the same denominator within one whole [for example, 5/7 + 1/7 = 6/7] compare and order unit fractions, and fractions with the same denominators solve problems that involve all of the above. 	
Year 4	Fractions To count in hundredths, To write mixed number fractions. To show mixed number fractions on a number line. To find equivalent fractions. To find equivalent fractions (further practise). To simplify mixed number fractions. To simplify improper fractions. To add fractions. To add fractions (recording answers as a mixed number). To add fractions (simplest form). To subtract fractions. To subtract fractions (equivalence).	All of the above, plus: eighth sixth fifth twentieth proportion in every for every decimal decimal fraction decimal place simplify mixed number fraction improper fraction

	• To solve word problems.	decimal
		hundredths
	Decimals	
	• To record tenths.	
	• To record in tenths.	
	• To record in tenths (in different ways).	
	To write hundredths.	
	• To write hundredths.	
	• To write hundredths (in different ways).	
	To record hundredths.	
	 To write decimal numbers. 	
	 To compare and order decimal numbers. 	
	To create number sequences.	
	To round decimal numbers.	
	 To write fractions as decimal numbers. 	
	• To divide whole numbers by 10.	
	• To divide whole numbers by 100.	
	/4 National Curriculum – End Point:	
	Pupils will be taught to:	
	 recognise and show, using diagrams, families of common equivalent fractions 	
	- count up and down in hundredths; recognise that hundredths arise when dividing an object by one hundred and	
	dividing tenths by ten.	
	- solve problems involving increasingly harder fractions to calculate quantities, and fractions to divide quantities,	
	including non-unit fractions where the answer is a whole number	
	- add and subtract fractions with the same denominator	
	 recognise and write decimal equivalents of any number of tenths or hundredths 	
	- recognise and write decimal equivalents to $\frac{1}{4}$, $\frac{1}{2}$, $\frac{3}{4}$	
	- find the effect of dividing a one- or two-digit number by 10 and 100, identifying the value of the digits in the answer	
	as ones, tenths and hundredths	
	 round decimals with one decimal place to the nearest whole number 	
	- compare numbers with the same number of decimal places up to two decimal places	
	 solve simple measure and money problems involving fractions and decimals to two decimal places 	
Year 5	Fractions	All of the above, plus
		reduced to

• To divide whole numbers to create fractions; to create mixed numbers and improper fractions when dividing whole	cancel
numbers.	ninth
 To write improper fractions and mixed numbers using a number line and pictorial methods. 	twelfth
 To find equivalent fractions using pictorial methods. 	ratio
 To compare and order fractions using the pictorial method. 	to every
 To compare and order improper fractions using the pictorial method. 	as many as percentage
 To compare mixed numbers using pictorial representations; to find common denominators where one fraction is 	%
already the common denominator for all fractions in the question.	per cent
 To make number pairs (number bonds) with fractions with different denominators. 	convert
 To add unlike fractions by finding a common denominator using pictorial methods. 	
 To add together unlike fractions where the sum is greater than 1, creating mixed numbers or improper fractions. 	
 To add unlike fractions which create improper fractions and mixed numbers that give rise to simplification. 	
 To subtract fractions with different denominators; to subtract fractions from whole numbers. 	
• To subtract fractions where the denominators are not the same; to use bar models as a key strategy for subtracting	
fractions.	
• To subtract fractions and mixed numbers from mixed numbers with different denominators.	
• To multiply fractions by whole numbers creating other fractions, mixed numbers or improper fractions	
 To multiply fractions by whole numbers where the product is an improper fraction or mixed number. 	
 To multiply mixed numbers by whole numbers, creating larger mixed numbers. 	
 To multiply mixed numbers by whole numbers in multi-step word problems. 	
Decimals	
• To write decimal numbers.	
• To read and write decimals.	
• To compare tenths and hundredths written as decimals.	
To order and compare decimals.	
• To compare and order decimals of amounts.	
• To write fractions as decimals.	
• To add and subtract amounts in decimals.	
 To add and subtract decimals; to add and subtract amounts in pounds and pence. 	
• To add and subtract amounts in pounds and pence.	
• To add and subtract decimals; to add and subtract amounts in pounds and pence.	
• To add and subtract decimals to find the smallest possible sum and difference.	
• To add and subtract decimals; to find number pairs that add up to 1.	
 To add and subtract the perimeter of an object using decimals. To round decimals to the nearest whole number; to round numbers to nearest tenth 	

 To compare quantities; to compare fractions, decimals and percentages; to convert fractions to decimals and 	
percentages.	
 To convert values of an amount into percentages; to convert fractions into percentages. 	
 To convert values of an amount into percentages; to convert fractions into percentages. 	
<u>Y5 National Curriculum – End Point:</u>	
Pupils will be taught to:	
 compare and order fractions whose denominators are all multiples of the same number 	
 identify, name and write equivalent fractions of a given fraction, represented visually, including tenths and hundredths 	
 recognise mixed numbers and improper fractions and convert from one form to the other and write mathematic statements > 1 as a mixed number [for example, 2/5 + 4/5 = 6/5 = 1 1/5] 	cal
- add and subtract fractions with the same denominator and denominators that are multiples of the same numbe	er
- multiply proper fractions and mixed numbers by whole numbers, supported by materials and diagrams	
 read and write decimal numbers as fractions [for example, 0.71 = 71/100] 	
 recognise and use thousandths and relate them to tenths, hundredths and decimal equivalents 	
 round decimals with two decimal places to the nearest whole number and to one decimal place 	
 read, write, order and compare numbers with up to three decimal places 	
 solve problems involving number up to three decimal places 	
 recognise the per cent symbol (%) and understand that per cent relates to 'number of parts per hundred', and w 	vrite
percentages as a fraction with denominator 100, and as a decimal	
 solve problems which require knowing percentage and decimal equivalents of ½, ¼, 1/5, 2/5, 4/5 and those fra 	actions
with a denominator of a multiple of 10 or 25.	
Fractions	All of the above, plus
• To use concrete materials to simplify fractions; to recognise equivalence in fractions to 1/4.	orial thousandth
 To simplify fractions using division and common factors; to represent fractions using concrete materials and pictors 	
representations.	
To compare fractions and place them in order from smallest to largest.	
To compare and order fractions by finding common denominators.	
 To compare and order fractions using common factors. To add and subtract unlike fractions; using pictorial representations to compare fractions and add/subtract. 	

•	To add and subtract mixed numbers, including fractions with different denominators; to subtract from the whole and
	add the remainder back on.
•	To add and subtract fractions with different denominators; to add and subtract mixed numbers.
•	To multiply fractions using pictorial representations and abstract methods.
•	To determine if the commutative law applies to fractions; to multiply fractions using concrete materials and pictorial
	representations.
•	To use concrete materials to understand and solve the multiplication of fractions; to simplify equations using pattern
	blocks.
•	To divide a fraction by a whole number; to use pictorial representation to divide whole numbers into fractions.
•	To divide fractions by whole numbers using concrete materials and pictorial representations; to divide fractions when
	the numerator and divisor are not easily divisible.
•	To divide fractions by a whole number; to use pictorial representations to support division.
Decima	
•	To read and write decimals to thousandths; to use concrete materials to represent decimals.
•	To divide whole numbers by larger whole numbers; to use Base 10 materials to represent tenths, hundredths and
	thousandths.
•	To divide whole numbers that give rise to decimals; to calculate decimal fraction equivalents using long division.
•	To convert fractions into decimals using bar models and long division.
•	To write fractions as decimals; to use long division as the key strategy for turning fractions into decimals.
•	To multiply decimals by whole numbers using partitioning or the worded method to help find the solution.
•	To multiply whole numbers that include a decimal by other whole numbers; to use partitioning and the worded
	method as key strategies.
•	To multiply decimals by whole numbers, including regrouping and renaming.
•	To multiply decimals by whole numbers using a variety of methods; to use the heuristic 'making a list' to help solve a
	problem.
•	To divide decimals using number bonds and number discs as the key strategies.
•	To divide decimals using bar models, number bonds and long division as key strategies, including regrouping and
	renaming.
•	To multiply decimals by a 2-digit whole number using number discs and the column method.
•	To divide decimals by 2-digit numbers using number bonds and the worded method.
•	To divide decimals by 2-digit whole numbers using number bonds and the worded method.
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Percent	
•	To find the percentage of a whole number using division and multiplication; to use bar modelling as a pictorial
	approach to calculating percentage.

•	To find the percentage of a quantity; to use bar model diagrams to support the division and multiplication of numbers
	towards the percentage.
•	To find the percentage change in an amount over time; to calculate the percentage change where the number gives
	rise to a decimal.
•	To use percentage, bar models and fractions to compare amounts.
Ratio	
•	To use ratios and fractions to compare objects; to find the relationship between ratios, percentages and fractions.
٠	To determine the ratio of a quantity using concrete materials; to simplify ratios using concrete materials in addition to
	division.
•	To compare more than two quantities using the term 'ratio'; to use bar models to express ratios where there is more
	than one quantity.
•	To compare quantity using both fractions and ratios; to use bar model diagrams to represent ratios.
•	To compare quantities using bar models and common factors; to use multiplication and division to simplify ratios.
•	To compare numbers using ratios; to make decisions about simplifying ratios using division.
•	To solve word problems using a variety of heuristics including guess-and-check and bar models; to apply knowledge of
	ratios to word problems.
•	To solve word problems using the bar model heuristic; to employ division and multiplication as primary strategies
	when solving word problems visually.
٠	To apply the guess-and-check and advanced bar model heuristic to ratio word problems.
<u>Y6 Nati</u>	onal Curriculum – End Point:
Pupils v	/ill be taught to:
-	use common factors to simplify fractions; use common multiples to express fractions in the same denomination
-	compare and order fractions, including fractions > 1
-	add and subtract fractions with different denominators and mixed numbers, using the concept of equivalent fractions
-	multiply simple pairs of proper fractions, writing the answer in its simplest form [for example, $\frac{1}{4} \times \frac{1}{2} = \frac{1}{8}$]
-	divide proper fractions by whole numbers [for example, $1/3 \div 2 = 1/6$]
-	associate a fraction with division and calculate decimal fraction equivalents [for example, 0.375] for a simple fraction
	[for example, 3/8]
-	identify the value of each digit in numbers given to three decimal places and multiply and divide numbers by 10, 100
	and 1000 giving answers up to three decimal places
	multiply one-digit numbers with up to two decimal places by whole numbers
-	use written division methods in cases where the answer has up to two decimal places
-	solve problems which require answers to be rounded to specified degrees of accuracy

- recall and use equivalences between simple fractions, decimals and percentages, including in different contexts.	